LONDON SCHOOL OF HYGIENE AND TROPICAL MEDICINE

28 March 2017

D.R.Cox Nuffield College, Oxford

• Formulation of research questions

• Planning of investigation

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- Metrology

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- Planning of investigation
- Metrology
- Collection of data

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- Metrology
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- Preliminary analysis

• Formulation of research questions

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- Formal analysis

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- Conclusions of analysis

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- Interpretation

Some types of dependence analysis of a single outcome on v explanatory variables measured on n individuals

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- Small *n* and large *v*, for example n = 40, v = 50,000
- Joint work with Heather Battey, Department of Mathematics, Imperial College

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Ridge regression

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